

$$F^{-1}(X) := P(Xt) \\ F^{-1}(U) = F(t).$$

$$P(F^{-1}(U)t) = P(F(F^{-1}(U))F(t)) = P(UF(t)) = F(t)$$

some

$$X_1, \dots, X_n$$

$$\{f_\theta :$$

$$\theta \in$$

$$\Theta\}$$

$$f_\theta$$

$$\Theta$$

$$R \times$$

$$[0, \infty)$$

$$\theta$$

$$(\mu, \sigma^2)$$

$$\{f_{\mu, \sigma^2}(x) : (\mu, \sigma^2) \in R^2, \mu \in R, \sigma^2 > 0\}.$$

$$Y$$

$$\theta$$

$$Y$$

$$\text{point}$$

$$\text{es-}$$

$$\text{ti-}$$

$$\text{ma-}$$

$$\text{tor}$$

$$\text{es-}$$

$$\text{ti-}$$

$$\text{ma-}$$

$$\text{tor}$$

$$X_1, \dots, X_{20}$$

$$20$$

$$\{f_\theta :$$

$$\theta \in$$

$$\Theta\}$$

$$\left\{ \frac{1}{2\pi\sigma} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right) : \mu \in R, \sigma^2 > 0 \right\}.$$

$$\frac{\mu}{X} :=$$

$$(X_1 +$$

$$\dots +$$

$$X_{20})/20$$

$$X_1 +$$

$$X_2$$

$$\sigma^2$$

$$\frac{1}{19} \sum_{i=1}^{20} (X_i - \bar{X})^2.$$

$$X_1, \dots, X_n$$

$$\{f_\theta :$$

$$\theta \in$$

$$\Theta\}$$

$$Y =$$

$$t(X_1, \dots, X_n)$$

$$g(\theta)$$

$$\mu$$

$$\mu^2$$

$$\mu$$

$$t :$$

$$R^n \rightarrow$$

$$R^k$$

$$g :$$

$$\theta \rightarrow$$

$$R^k$$

$$Y$$

$$\text{un-}$$

$$\text{bi-}$$

$$\text{ased}$$

$$E_\theta(Y) = g(\theta) \text{ for all } \theta \in \Theta.$$

$$[n$$